

Сверхизолятор и топологический фазовый переход Березинского-Костерлица-Таулесса

Миронов Алексей Юрьевич

ИФП СО РАН

Всероссийская конференция Физика ультрахолодных атомов
19 - 21 декабря 2016 года

1. Введение. Топологические фазовые переходы.
2. Сверхпроводник и топологический фазовый переход.
3. Сверхизолятор и топологический фазовый переход.

Лауреаты Нобелевской премии по физике 2016 года

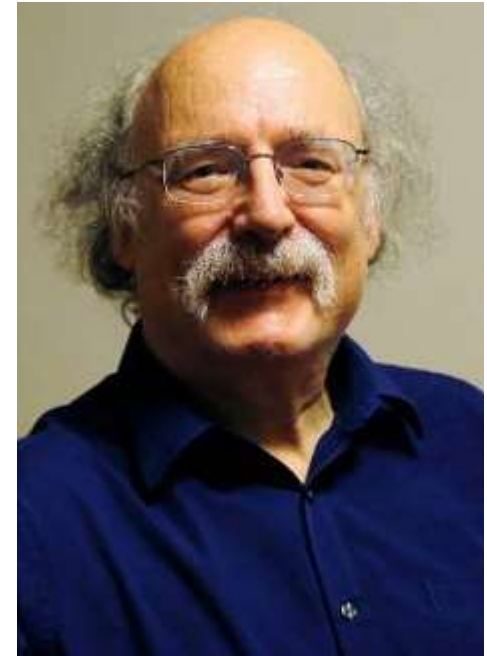
*за теоретические открытия
топологических фазовых переходов и топологических фаз материи*



Майкл Костерлиц
John Michael Kosterlitz



Дэйвид Таулесс
David James Thouless



Данкан Холдейн
Frederick Duncan
Michael Haldane

Фазовые переходы

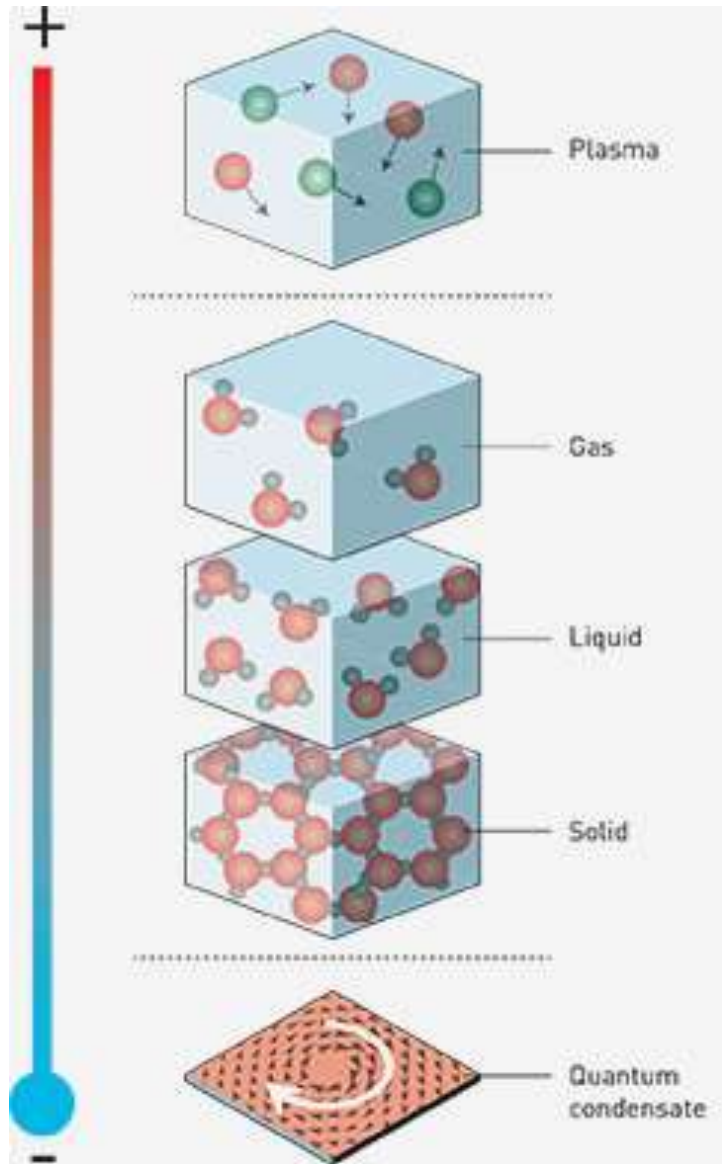


Illustration: ©Johan Jarnestad/The Royal Swedish Academy of Sciences



Топологические фазовые переходы

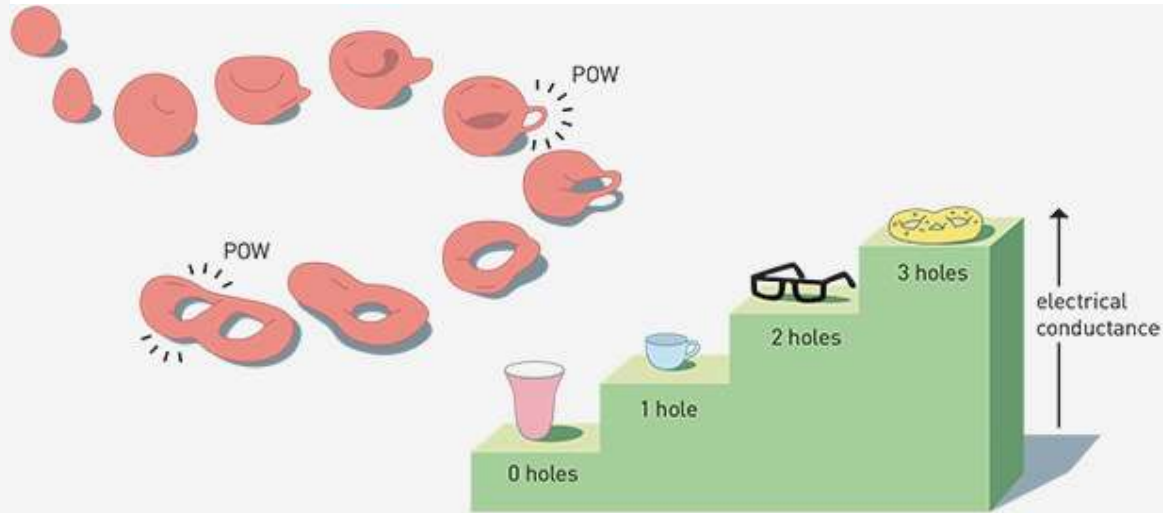
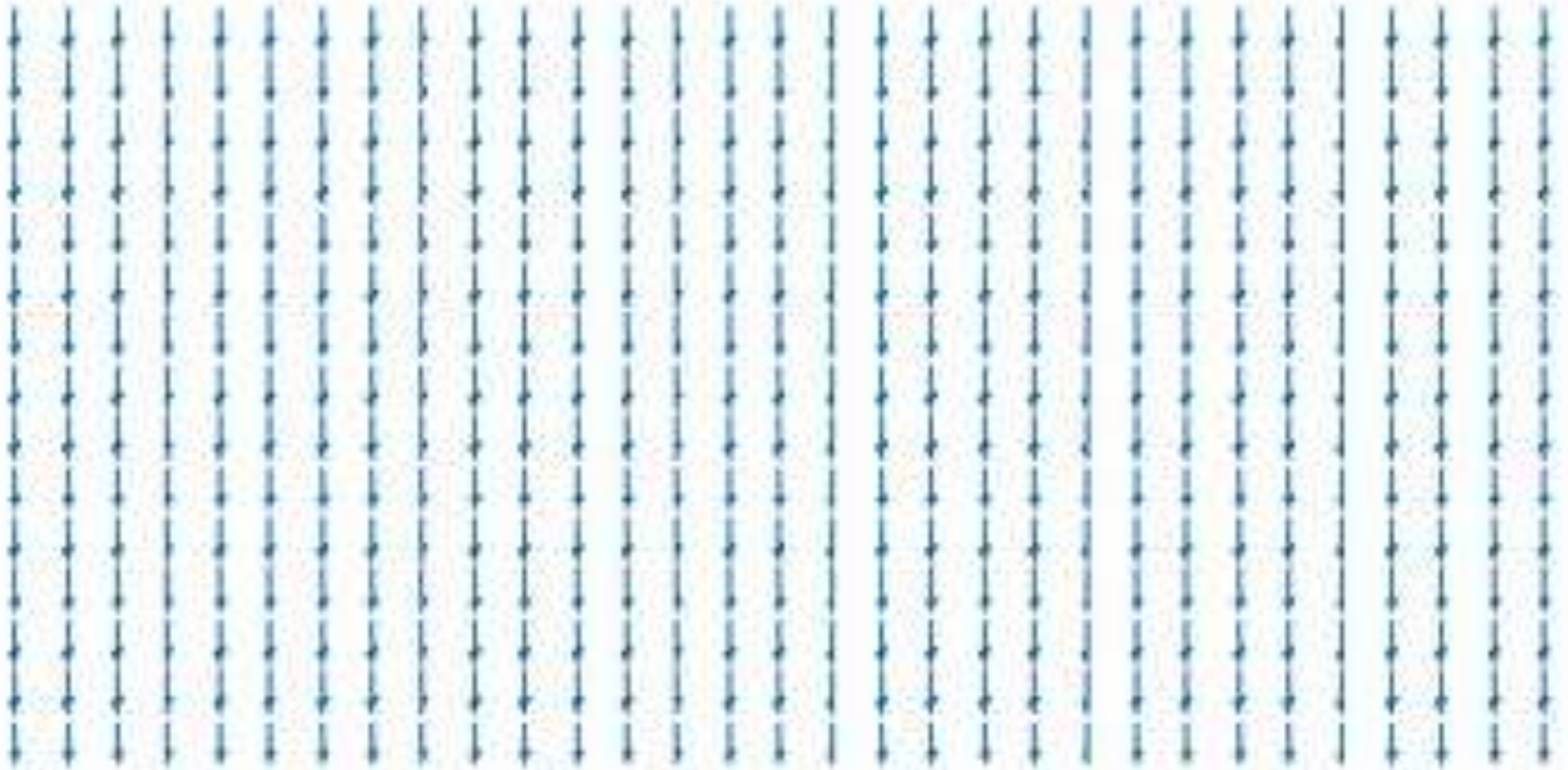


Illustration: ©Johan Jarnestad/The Royal Swedish Academy of Sciences

Рождение и исчезновение пары вихрь-антивихрь
Затрачиваемая энергия очень мала

(Березинский Вадим Львович, 1935-1980)

В.Л. Березинский, ЖЭТФ 59, 907 (1970); ЖЭТФ 61, 1144 (1971);



Топологический фазовый переход при повышении температуры
от газа практически не взаимодействующих связанных пар вихрь-антивихрь
к газу взаимодействующих вихрей
(Майкл Костерлиц, Дэвид Таулесс)

J.M. Kosterlitz and D. Thouless, J.Phys. C 6, 1181 (1973);

D.R. Nelson and J.M. Kosterlitz, Phys. Rev. Lett. 39, 1201 (1977)

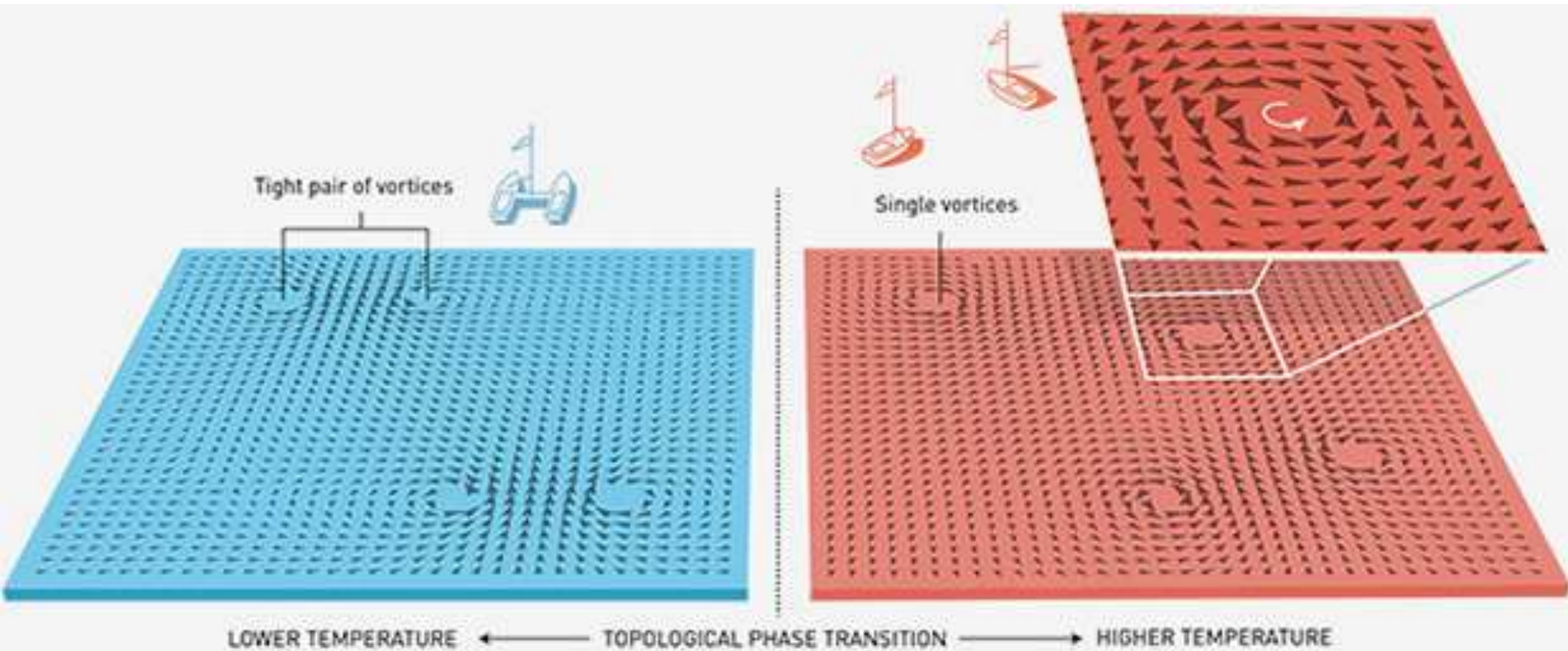


Illustration: ©Johan Jarnestad/The Royal Swedish Academy of Sciences

Топологический фазовый переход Березинского-Костерлица-Таулесса

Энергия взаимодействия вихрей:

$$U = E_0 \ln (R / r_0)$$

Энтропия:

$$S = 2k_B \ln (R / r_0)$$

(r_0 - размер ядра вихря)

Свободная энергия:

$$F = U - TS = E_0 \ln (R / r_0) - 2k_B T \ln (R / r_0)$$

Переход ВКТ при $T = T_{ВКТ} = E_0 / 2k_B$

Необходимо логарифмическое взаимодействие между элементами.

Сверхпроводимость и сверхизоляция

В ТОНКИХ ПЛЁНКАХ

на основе сверхпроводящих материалов

✓ Thin Disordered Superconducting films

quasi-2D:
electronic spectrum is 3D

$$l, l_F < d < \lambda, l_T$$

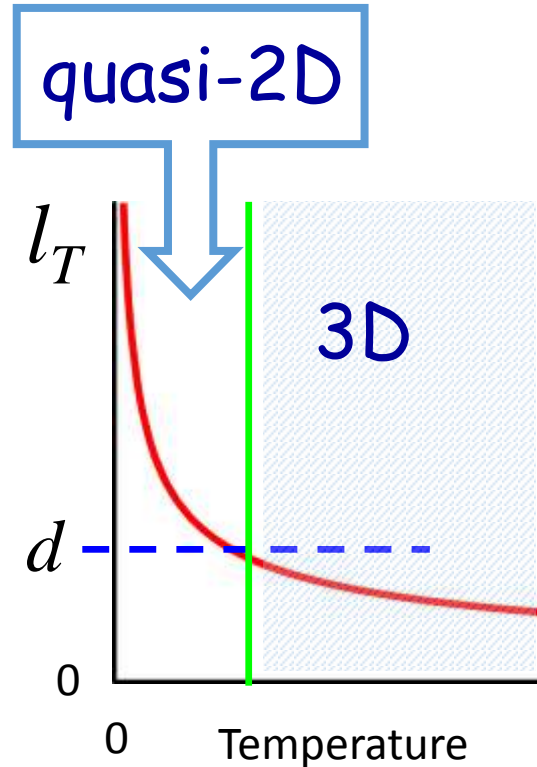
d - the thickness of the film

l - the mean free path

λ_F - Fermi wave length

ξ - the superconducting
coherence length

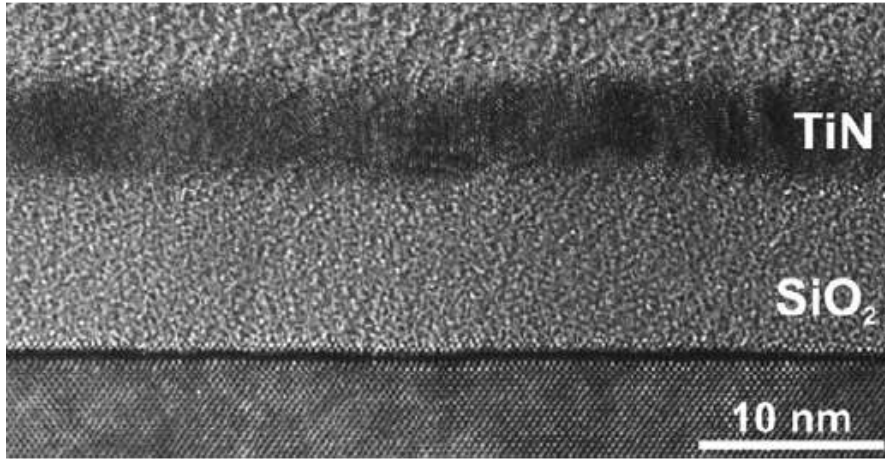
l_T - the thermal
coherence length



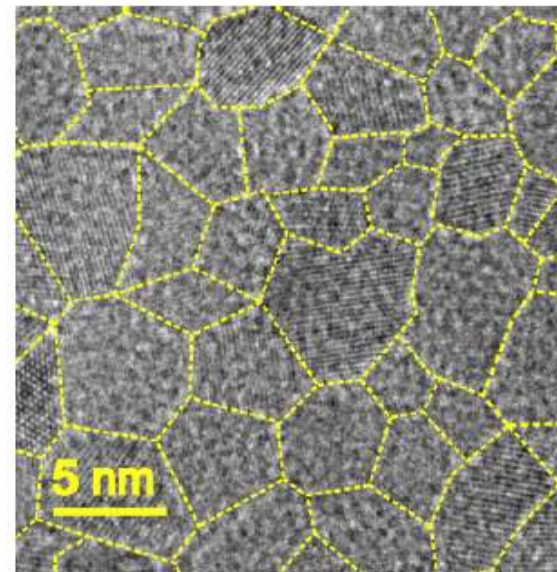
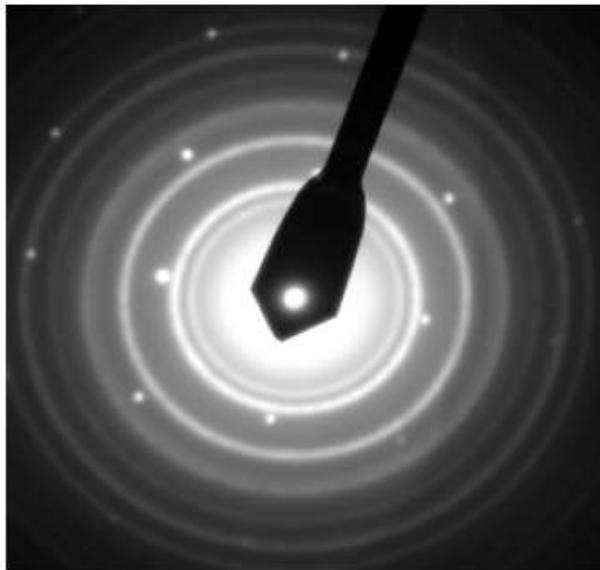
$$l_T = \sqrt{\frac{2\pi\hbar D}{k_B T}}$$

Experiment

TiN films

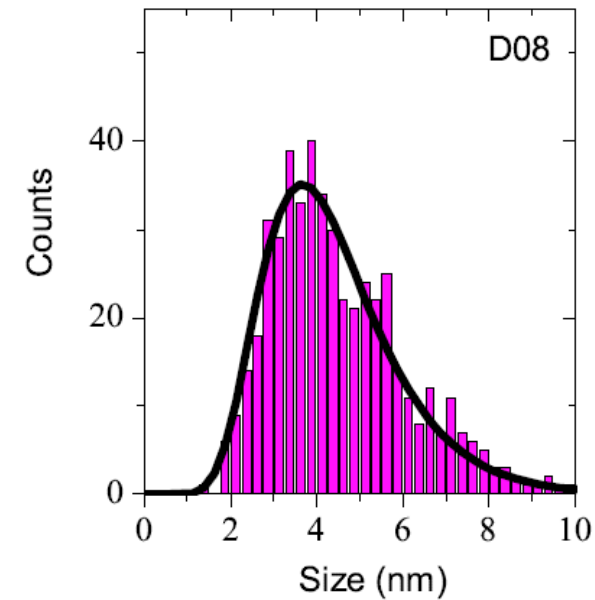
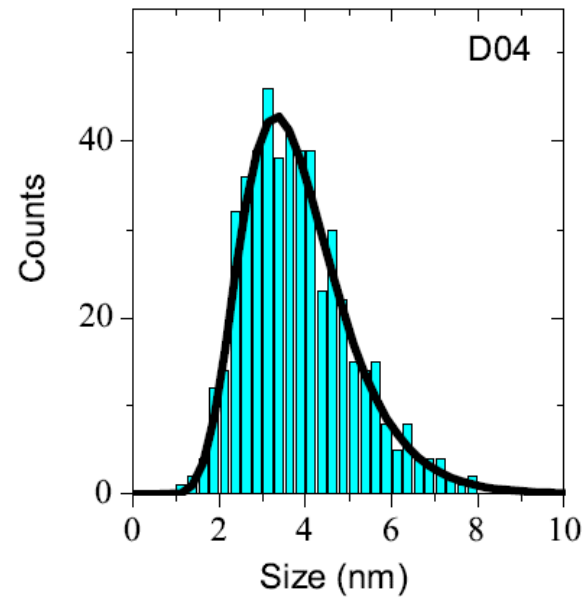
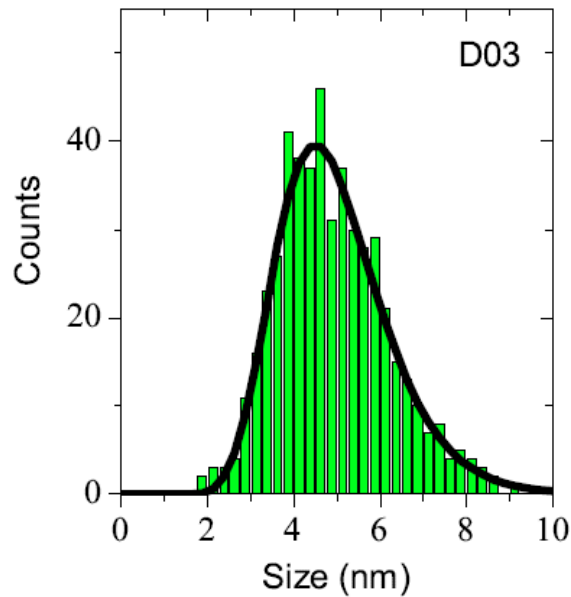


the thickness is 3.6 - 23 nm



✓ TiN films were formed by atomic layer deposition onto a Si/SiO₂ substrate at 400 °C.

Crystallites size distribution of the TiN films



The crystallites size distribution of films follows the lognormal distribution:

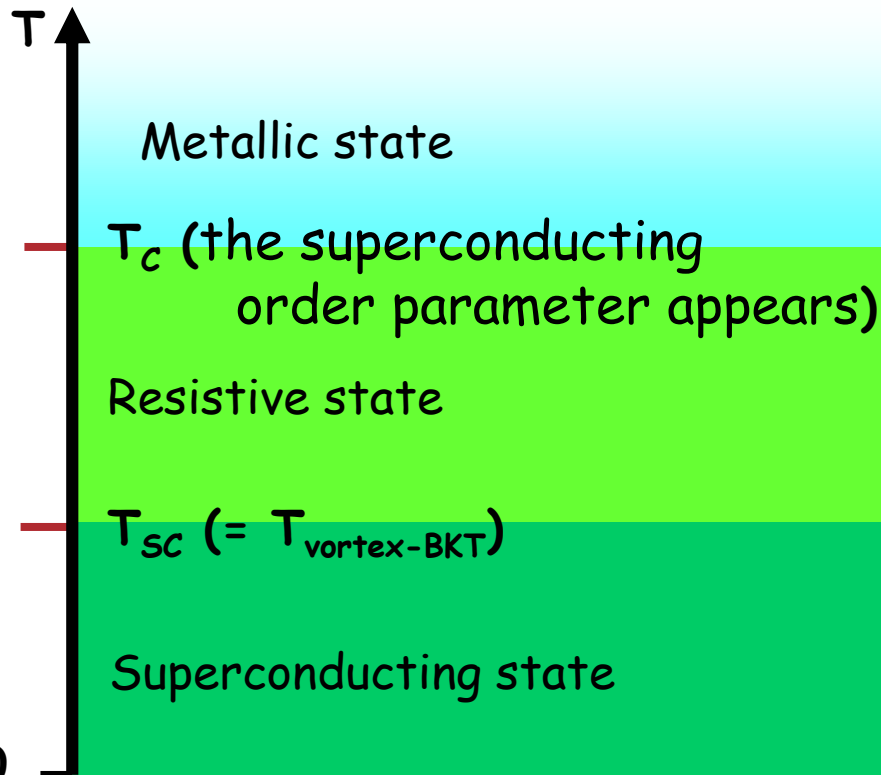
$$f(x) \propto \frac{1}{x\sigma\sqrt{2\pi}} \cdot e^{-\frac{(\ln x - \mu)^2}{2\sigma^2}}$$

The object

**! Two-dimensional superconducting systems:
2D JJ-array, granular films,
homogeneously disordered films**

Superconductor

$$\Psi = \Psi_0 \exp(i\varphi)$$



Drude conductivity
+ quantum corrections:
weak localization, e-e interaction,
superconducting fluctuations

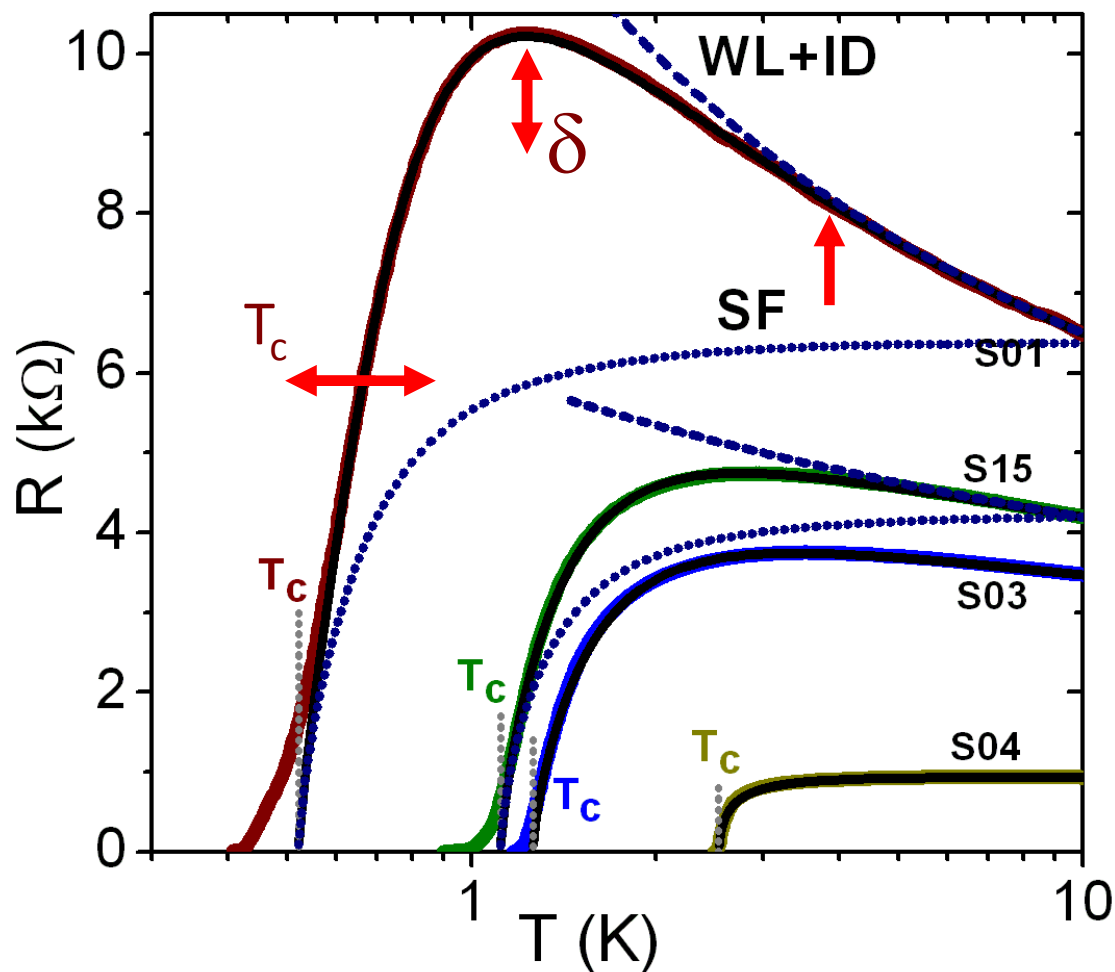
Absence of the global phase
coherence: a gas of unbound
vortices and antivortices

**Berezinskii-Kosterlitz-
Thouless transition**

Macroscopic phase coherence:
vortices and antivortices
are bound in pairs

TiN films

The fitting remarkably captures all major features of the observed dependences:
non-monotonic behaviour,
the position and value of R_{max} and T_{max} ,
the gradual decrease in the resistance.
We find that T_c lies at the foot of the $R(T)$ curves.



The determinations of T_c as the temperature where $R(T)$ drops to 0.9, 0.5 R_N significantly **overestimates** T_c .

Determination of T_{BKT}

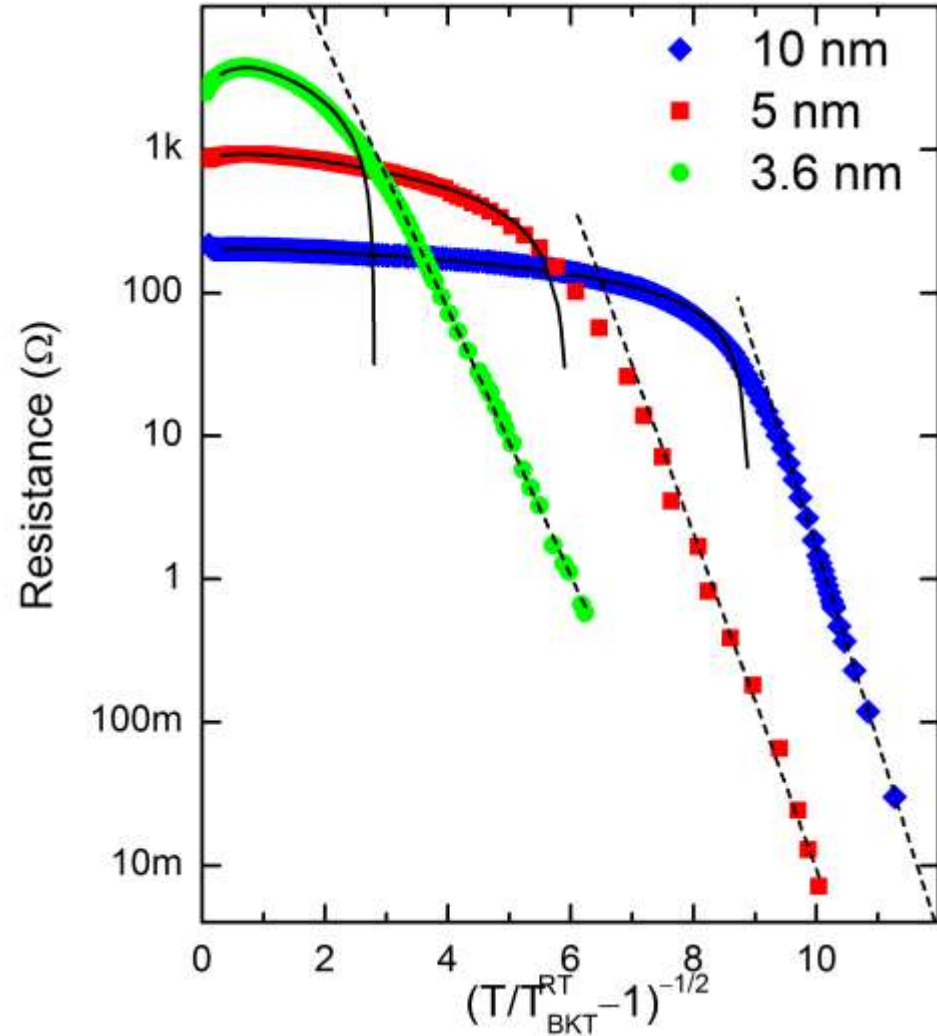
from linear conduction $T_{BKT} < T < T_c$

$$R(T) \propto \exp[-b(T/T_{BKT} - 1)^{-1/2}]$$

b is a constant of the order of unity

T_{BKT} is the only fitting parameter

$d, \text{ nm}$	3.6	5	10
$T_c, \text{ K}$	1.290	2.545	3.215
$T_{BKT}^{RT}, \text{ K}$	1.145	2.475	3.175
b	2.14	2.7	3.13



B. I. Halperin and D. R. Nelson,
J. Low. Temp. Phys. **36**, 599 (1979).
 S. Doniach and B. A. Huberman,
Phys. Rev. Lett. **42**, 1169 (1979).

The object

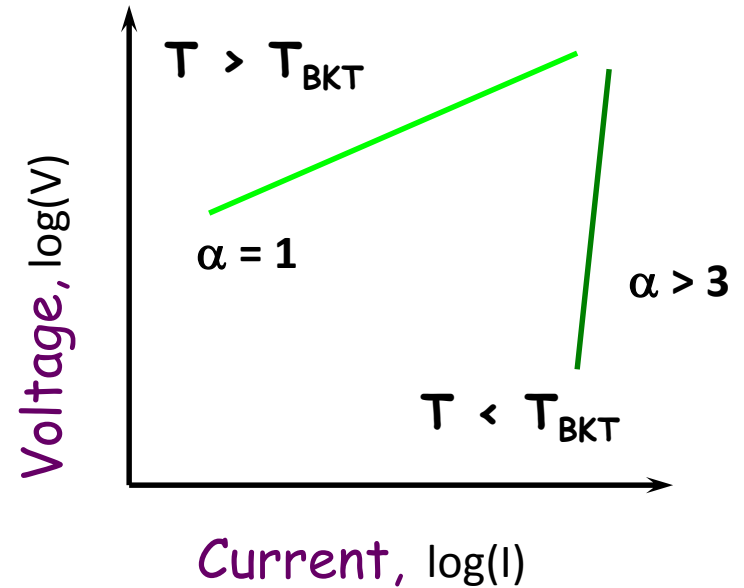
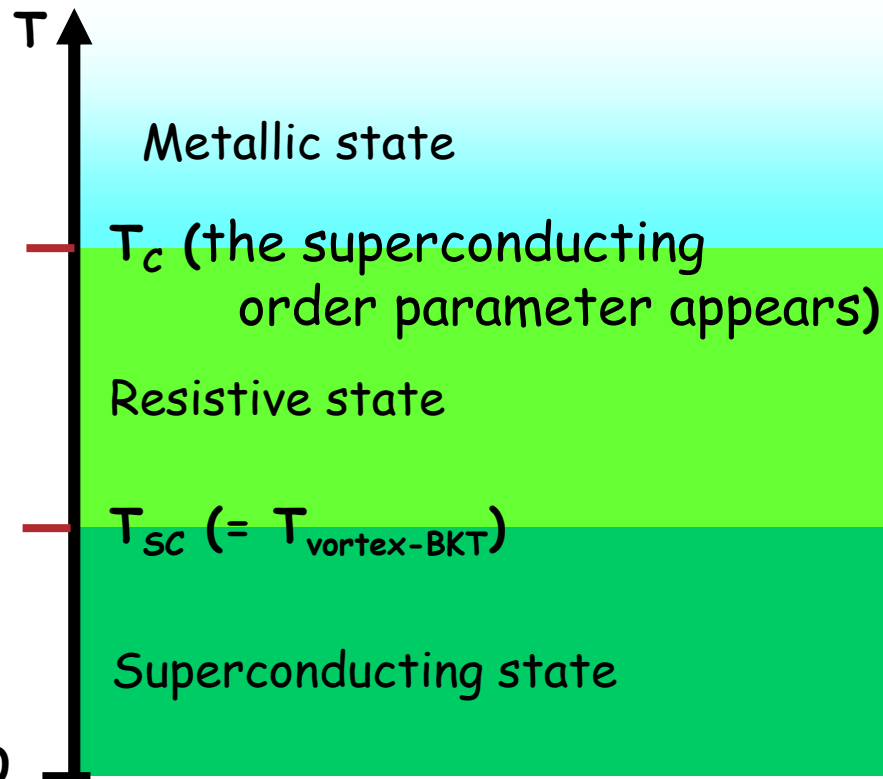
**! Two-dimensional superconducting systems:
2D JJ-array, granular films,
homogeneously disordered films**

Superconductor

$$\Psi = \Psi_0 \exp(i\varphi)$$

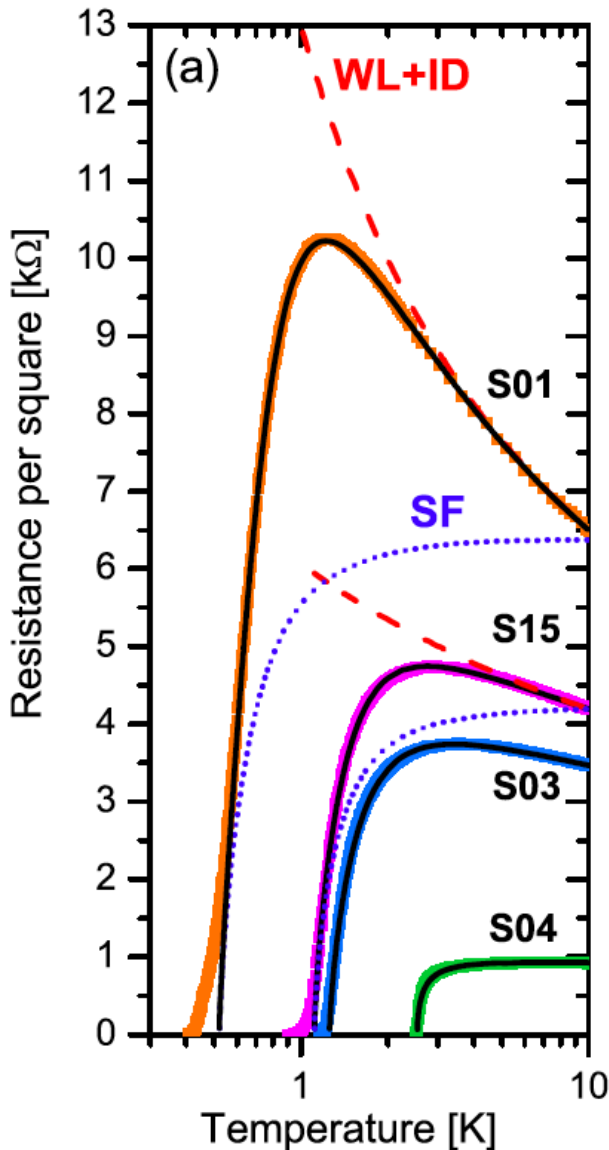
in experiment:

$$V \propto I^{\alpha(T)}$$

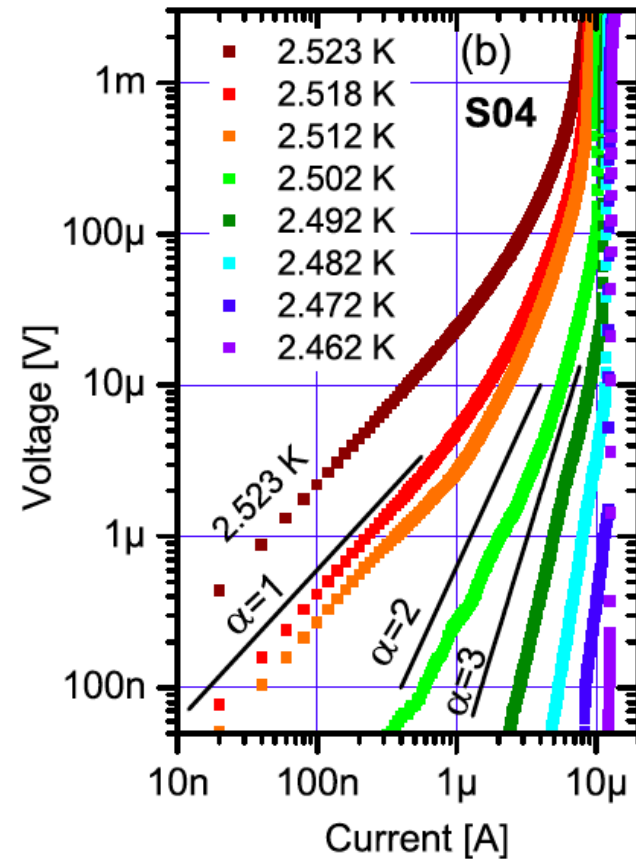
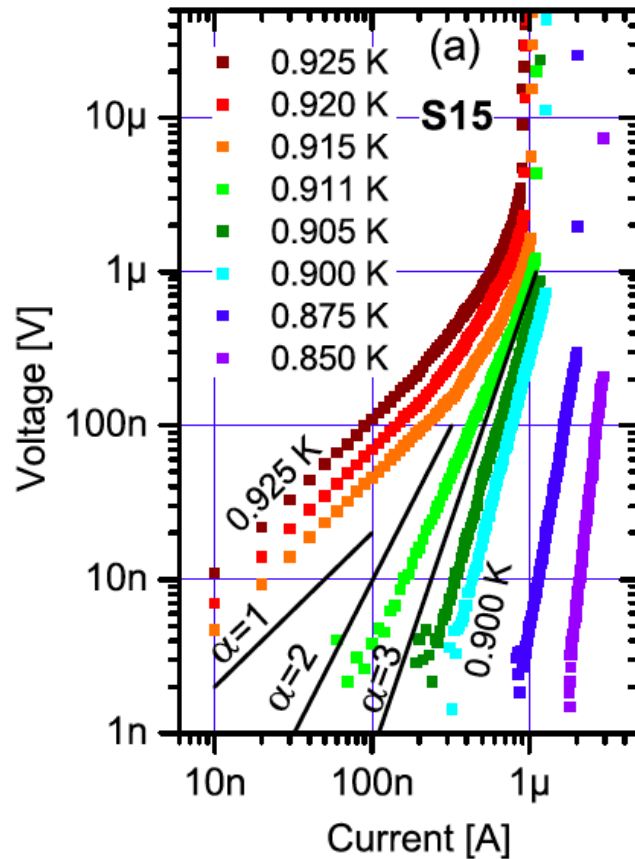


Vortex BKT transition

linear response regime



current - voltage characteristics $V \propto I^{\alpha(T)}$

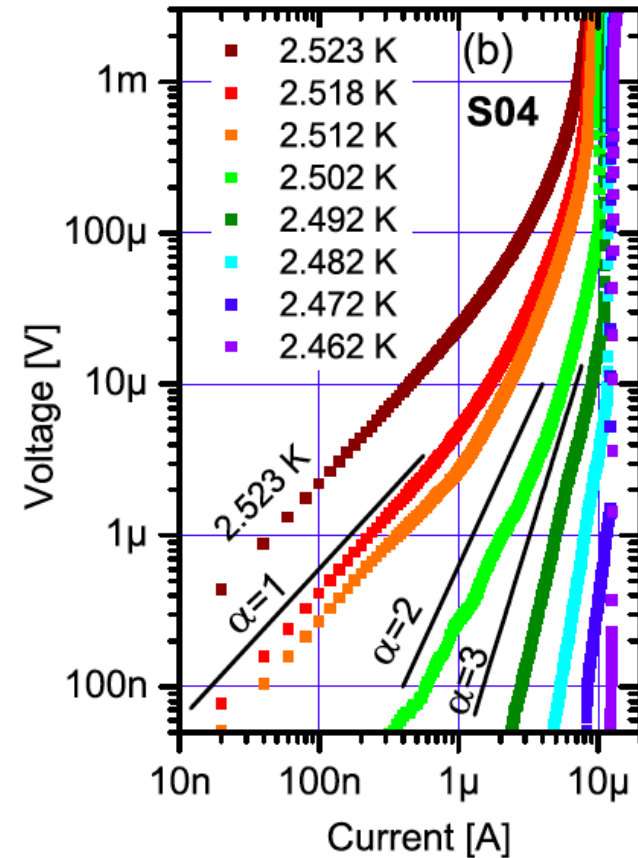
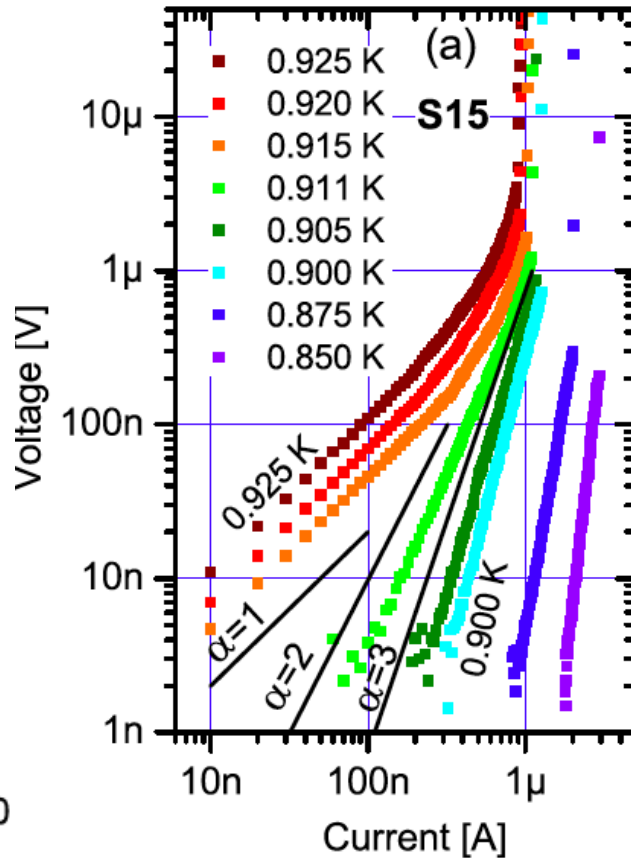
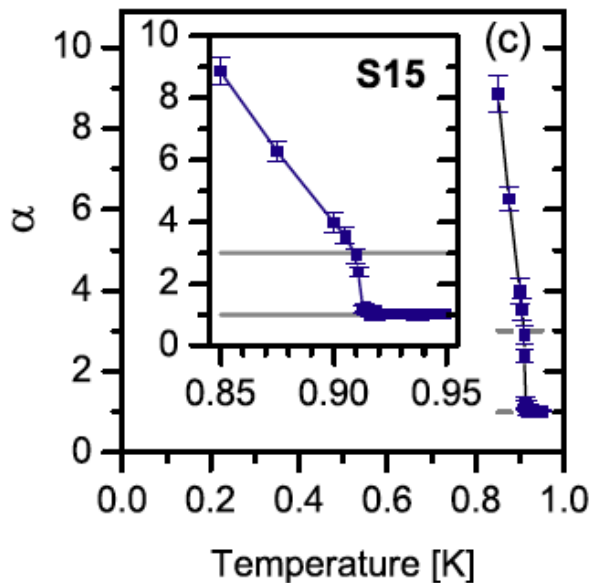


T. I. Baturina, S. V. Postolova, A. Yu. Mironov, A. Glatz, M.R. Baklanov, and V.M. Vinokur, EPL **97**, 17012 (2012).

Vortex BKT transition

current - voltage characteristics $V \propto I^{\alpha(T)}$

Characteristic jump
in the power exponent
at T_{BKT}

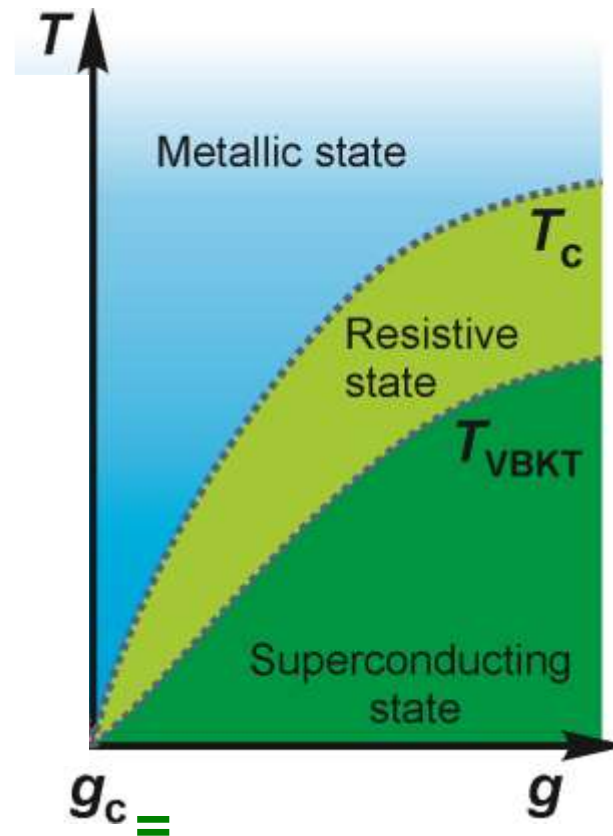


T. I. Baturina, S. V. Postolova, A. Yu. Mironov, A. Glatz, M.R. Baklanov, and V.M. Vinokur, EPL **97**, 17012 (2012).

Superconductor - Superinsulator Duality in two dimensions

Thermodynamic phase diagram

$V \rightarrow 0, I \rightarrow 0$



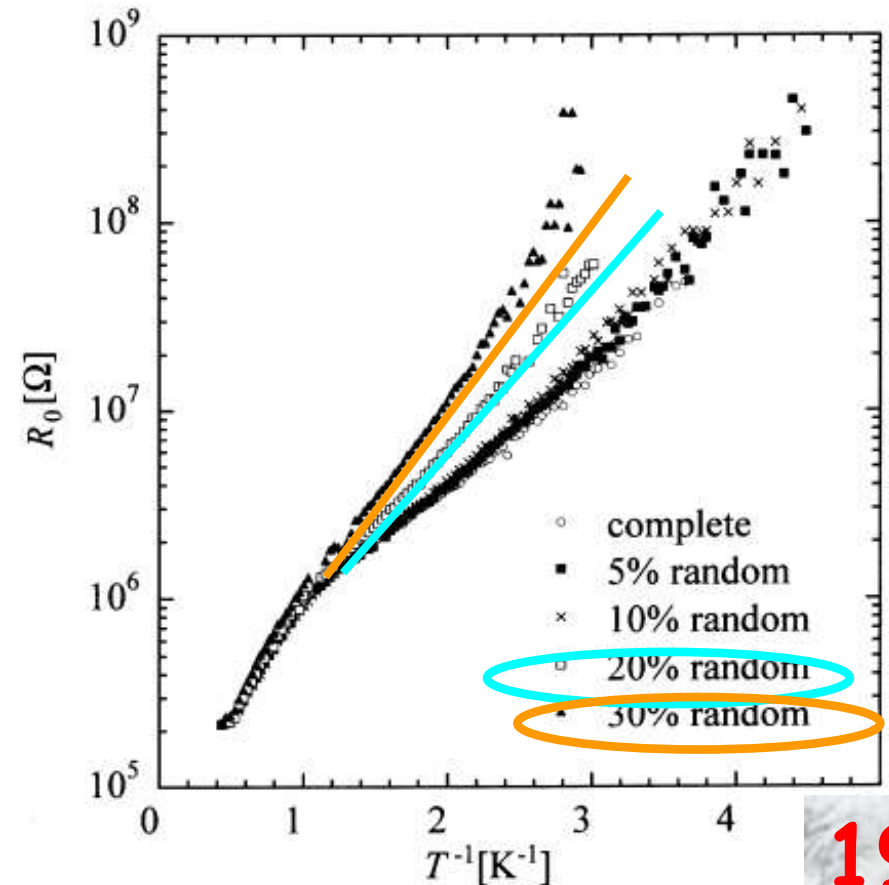
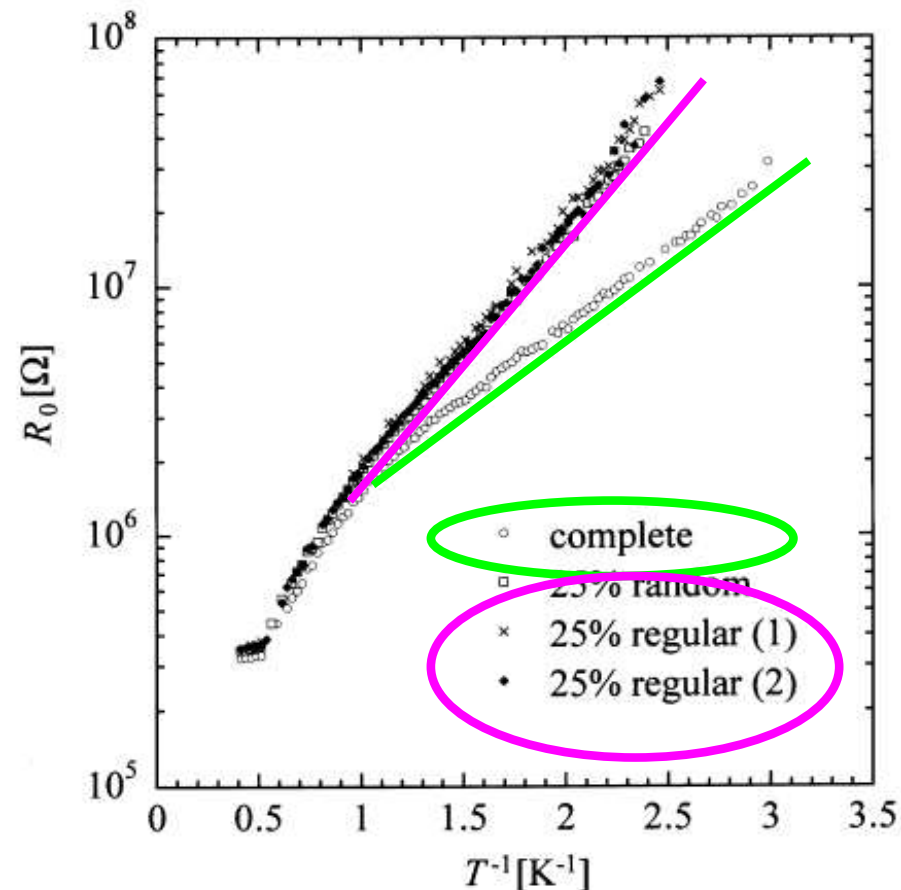
$$\Delta\varphi\Delta N \sim 1$$
$$\Delta\varphi = 0$$

the low-temperature
vortex-BKT phase

Two-Dimensional Arrays of Small Josephson Junctions with Regular and Random Defects

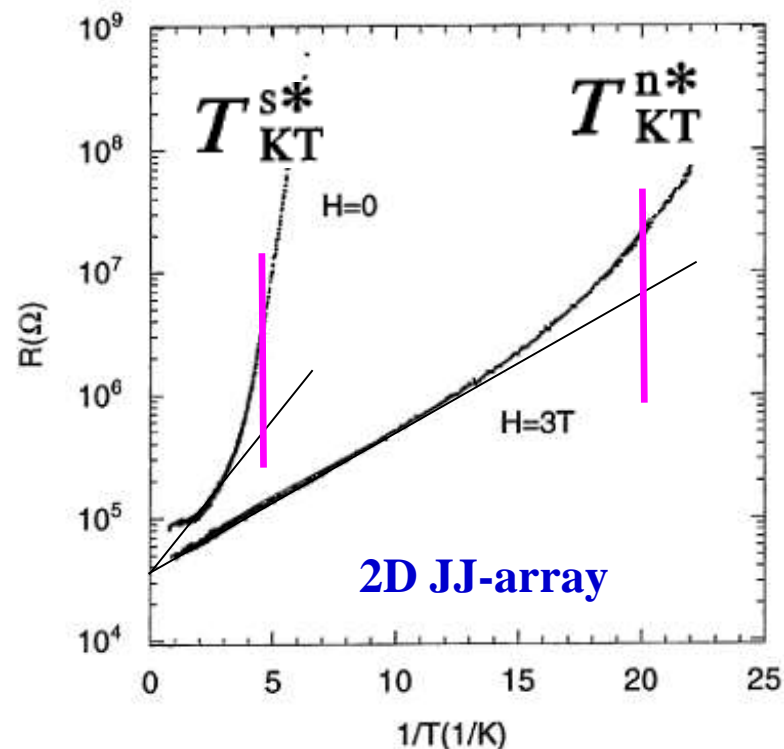
Takahide YAMAGUCHI, Ryuta YAGI, Shun-ichi KOBAYASHI and Youiti OOTUKA¹

We investigated the transport properties of two-dimensional arrays of small Josephson junctions of which a number of junctions are removed. We found that the more the number of removed junctions, the more rapidly the array resistance increases with decreasing temperature. The



Precursor of Charge KTB Transition in Normal and Superconducting Tunnel Junction Array

Akinobu KANDA and Shun-ichi KOBAYASHI



The array was 380 junctions in length and 331 junctions in width. Each junction had an area of $0.0072 (\mu\text{m})^2$, normal-state tunneling resistance $R_N=32 \text{ k}\Omega$ and the capacitance $C=1.1 \times 10^{-15} \text{ F}$. The self-capacitance of the island electrode was $5.1 \times 10^{-17} \text{ F}$.

$$T_{\text{KT}}^{\text{s}*} = (0.19 \pm 0.01) \text{ K} \quad e^* = 2e$$

$$T_{\text{KT}}^{\text{n}*} = (0.05 \pm 0.01) \text{ K} \quad e^* = e$$

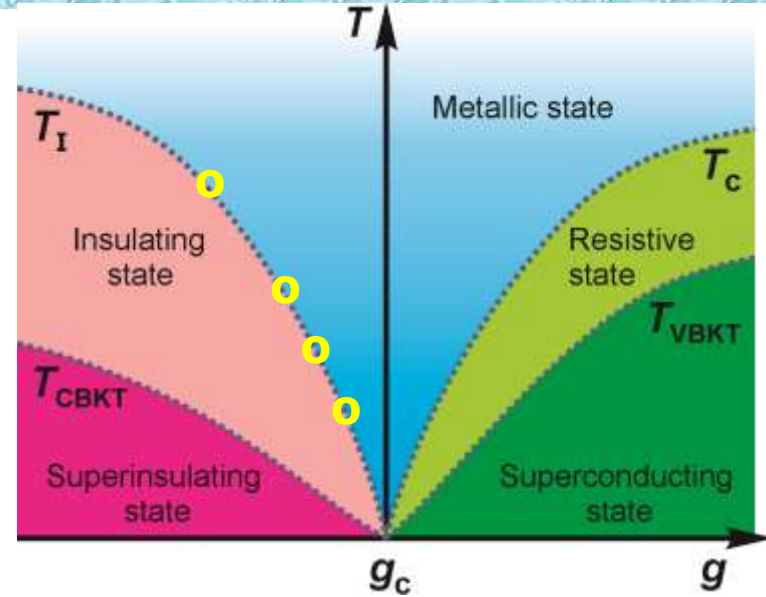
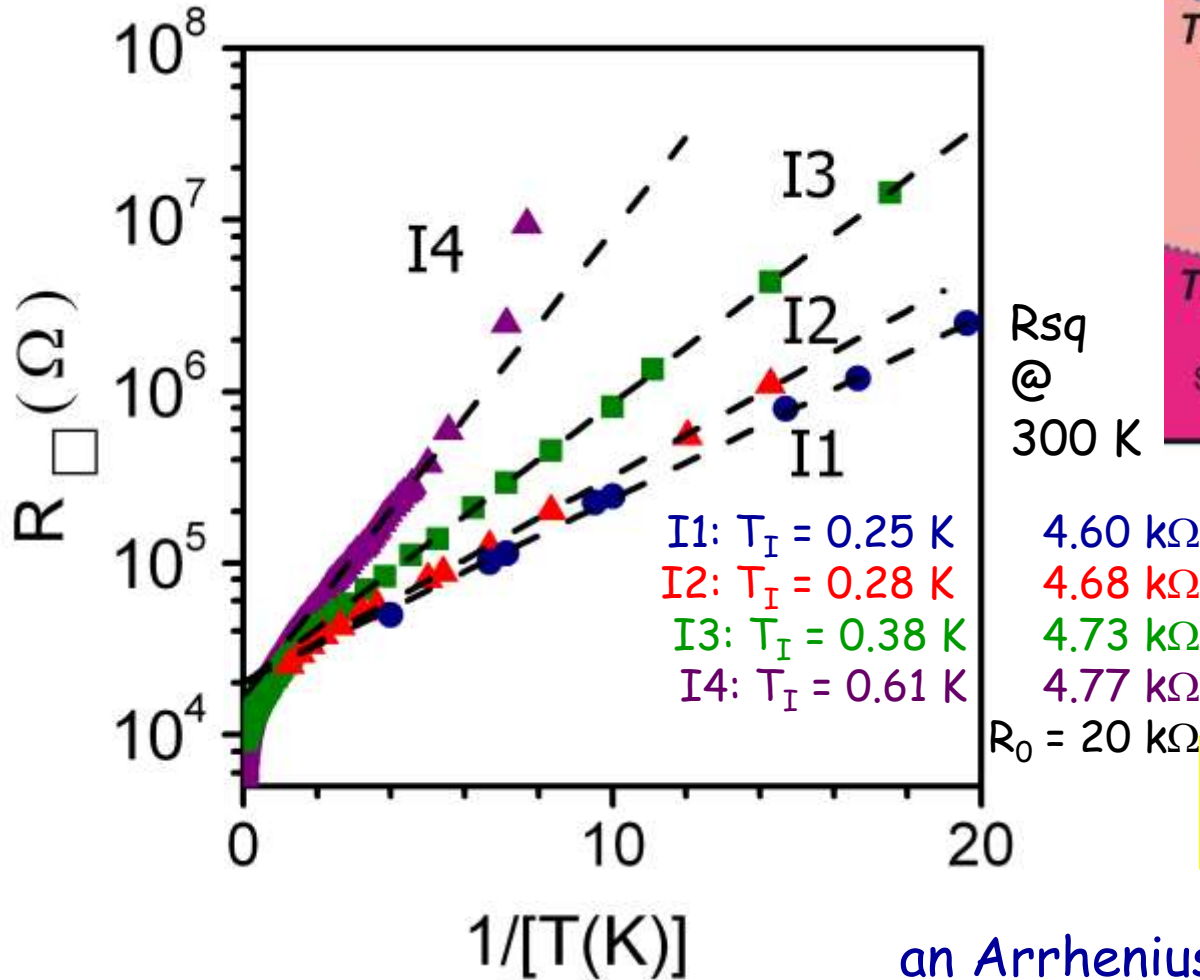
$$T_{\text{KT}}^{\text{s}*} / T_{\text{KT}}^{\text{n}*} \sim 4$$

Fig. 1. Resistance at $V=50 \mu\text{V}$ as a function of $1/T$ in $H=0$ and 3 T. Solid lines are results of fitting with eq. (1). The values of fitting parameters are $K=1.6$ and $b=1.0$ in $H=0$, and $K=1.6$ and $b=2.2$ in $H=3 \text{ T}$. For the values of T_{KT} , see the text.

$$k_{\text{B}} T_{\text{C-BKT}} = E_c = \frac{e^*}{2C}$$

Insulating side of the D-SIT in TiN films

At lower temperatures...



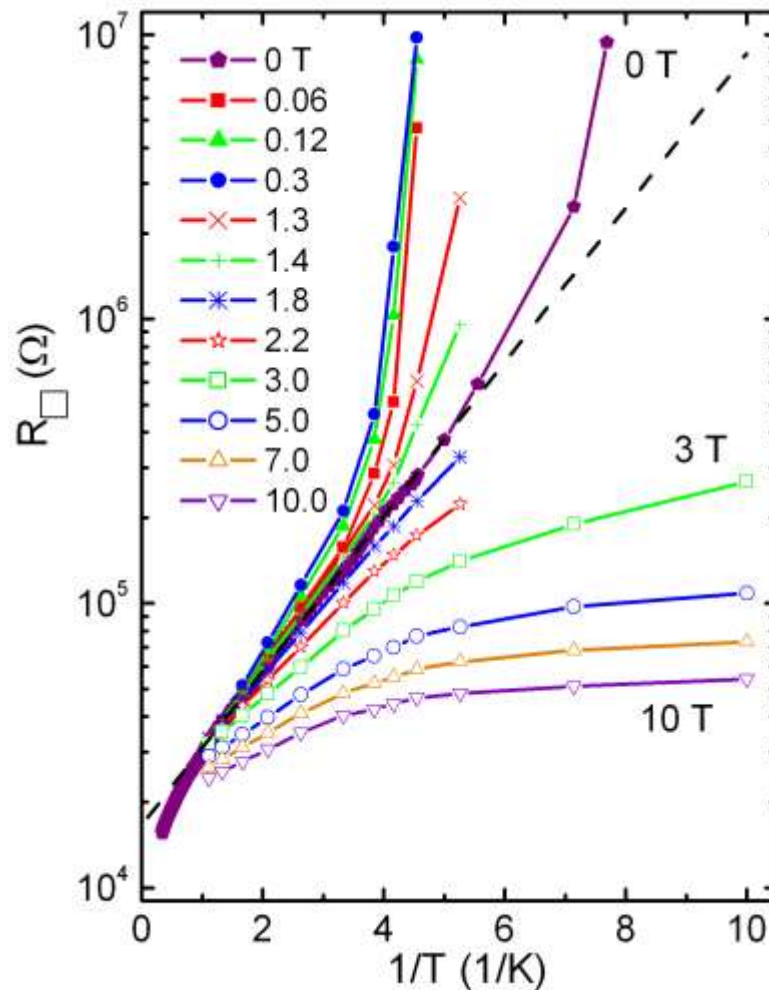
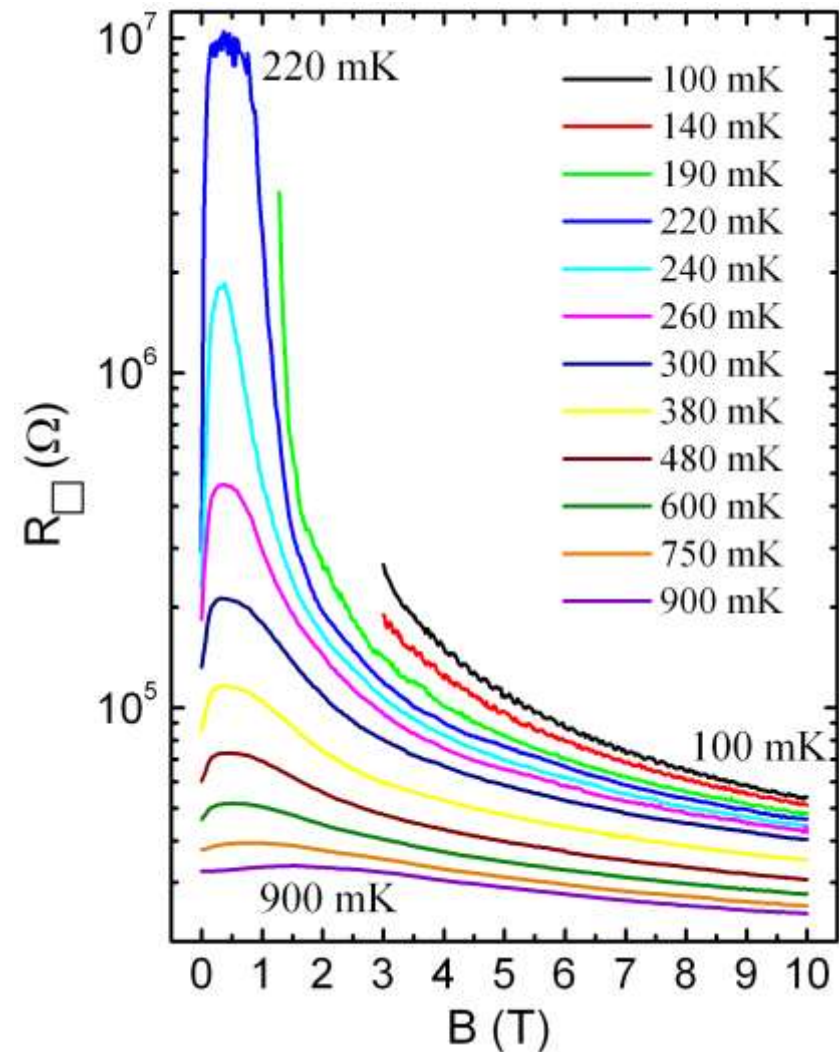
$$R = R_0 \exp(T_I/T)$$

an Arrhenius behavior of the resistance

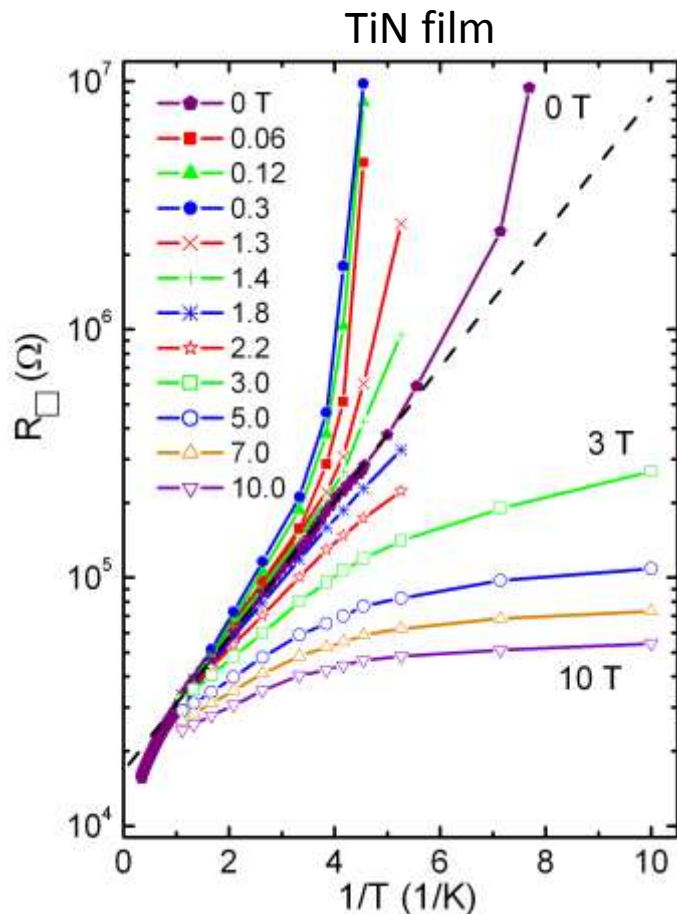
- T. Baturina, A.Yu. Mironov, V. Vinokur, M.R. Baklanov, C. Strunk, PRL 99, 257003 (2007)
- T. Baturina, A. Bilušić, A.Yu. Mironov, V. Vinokur, M.R. Baklanov, C. Strunk, Physica C 468, 316 (2008)
- T. Baturina, A.Yu. Mironov, V. Vinokur, M.R. Baklanov, C. Strunk, JETP Lett. 88, 752 (2008)

Hyperactivated behavior of the resistance

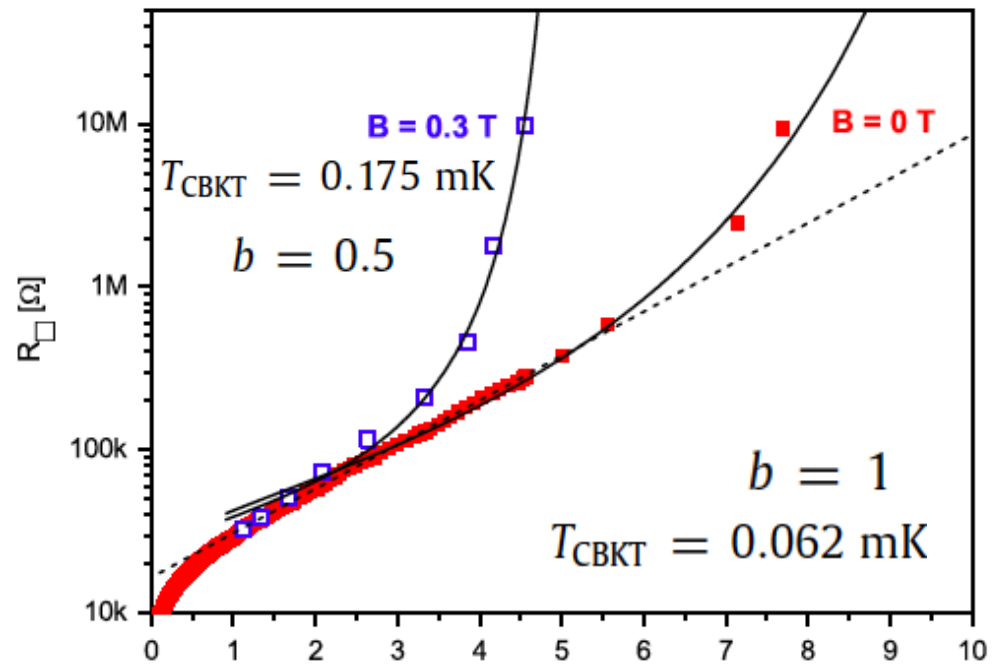
Arrhenius plots of the isomagnetic temperature dependences of the resistance.



Hyperactivated behavior of the resistance



T.I. Baturina, V.M. Vinokur / *Annals of Physics* 331 (2013) 236–257



$$R = R_0 \exp \left(A \exp \sqrt{\frac{b}{(T/T_{CBKT}) - 1}} \right)$$

$$R_0 = 8 \text{ k}\Omega$$

$$A = 1$$

T. Baturina, A.Yu. Mironov, V. Vinokur, M.R. Baklanov, C. Strunk,
JETP Lett. 88, 752 (2008)

T. Baturina & V. Vinokur, *Annals of Physics* 331, 236-257 (2013)

Arrhenius plot of the isomagnetic temperature dependences of the resistance

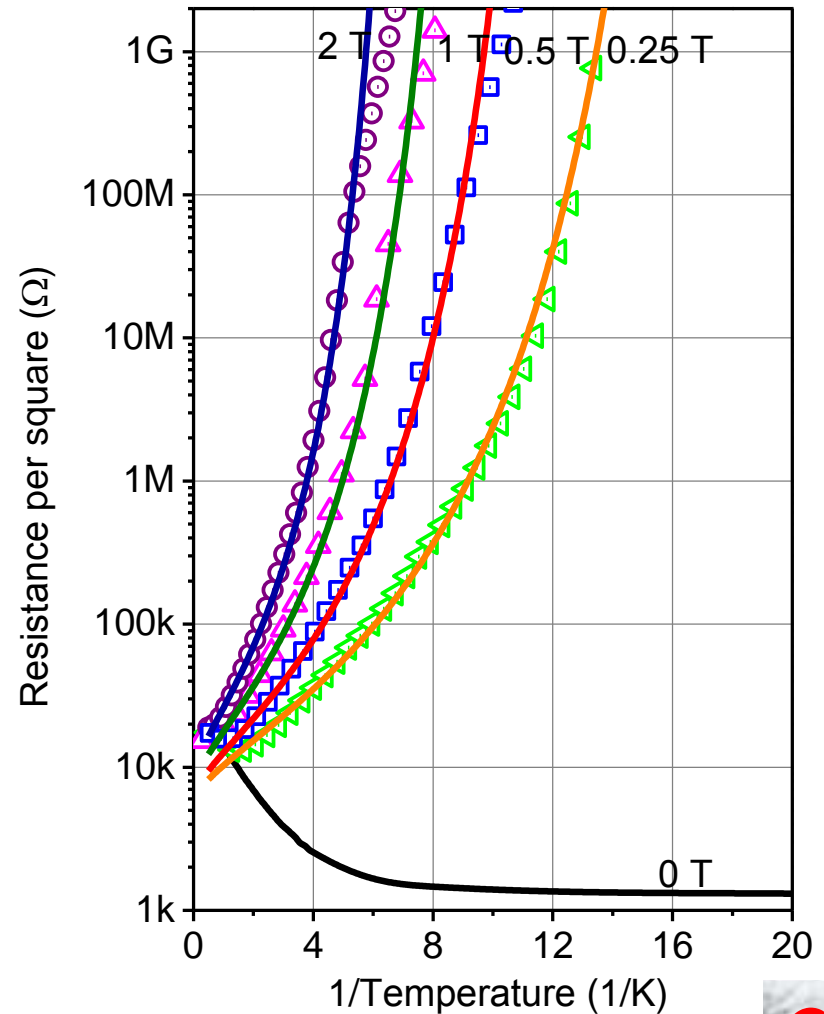
Hyperactivated behavior:
Resistance increases faster than that of the thermally activated type.

This indicates a change of the mechanism of the conductivity.

$$R = R_0 \exp \left(A \exp \sqrt{\frac{b}{(T/T_{CBKT}) - 1}} \right)$$

B	R ₀	T _{CBKT}
2 T	3000 Ω	90 mK
1 T	2500 Ω	70 mK
0.5 T	2100 Ω	54 mK
0.25 T	2000 Ω	39 mK

A = 1
b = 6



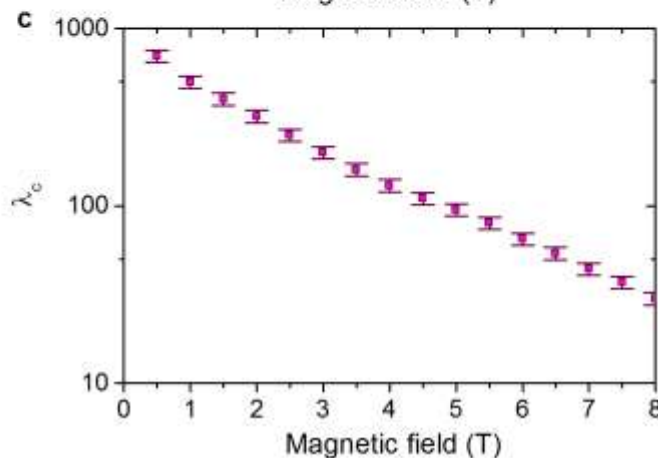
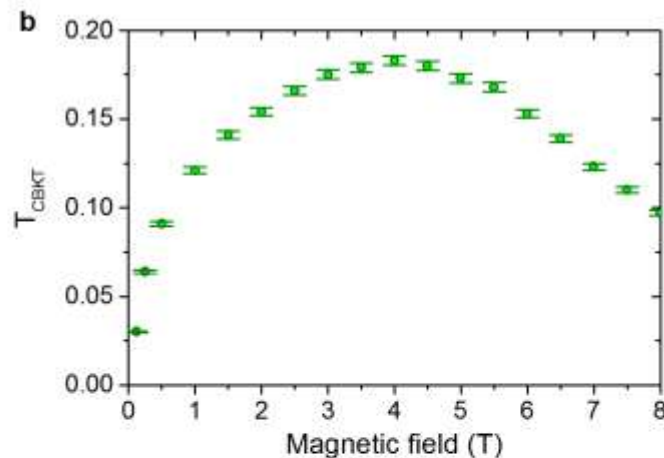
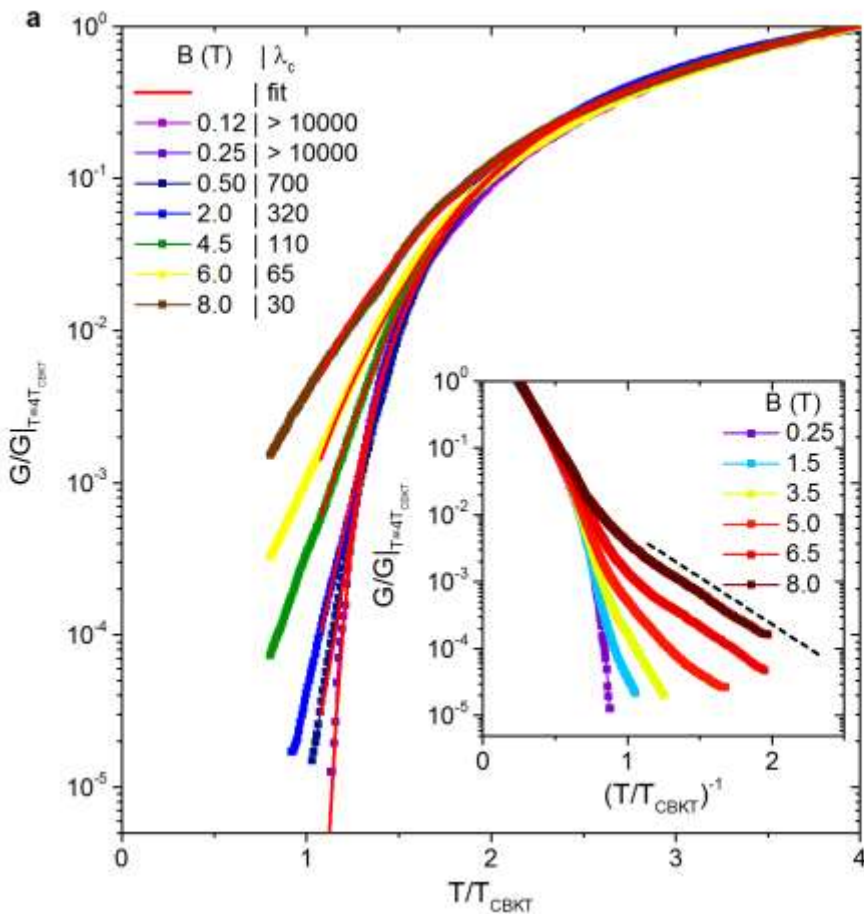
CBKT plot of the isomagnetic temperature dependences of the resistance

P. Minnhagen.

The two-dimensional Coulomb gas, vortex unbinding, and superfluid-superconducting films.

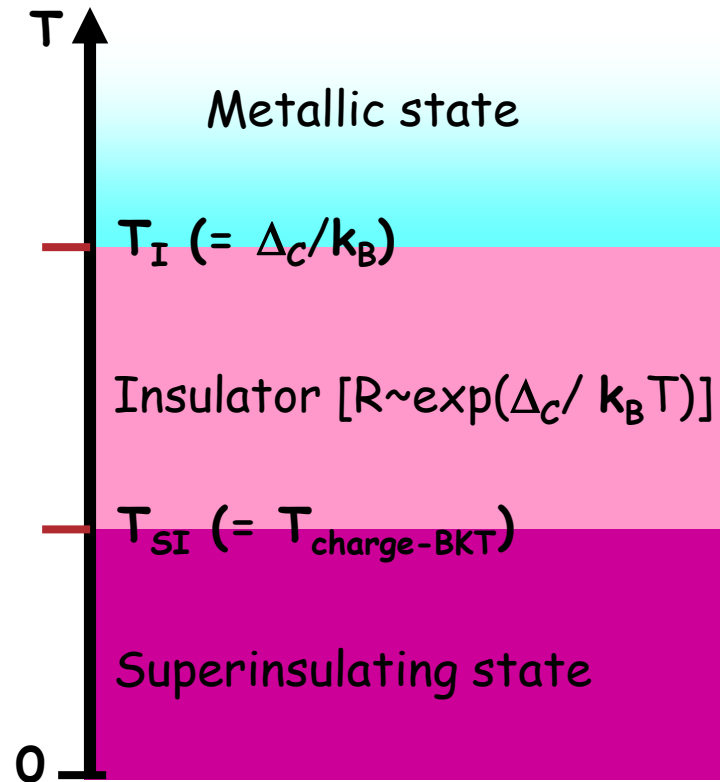
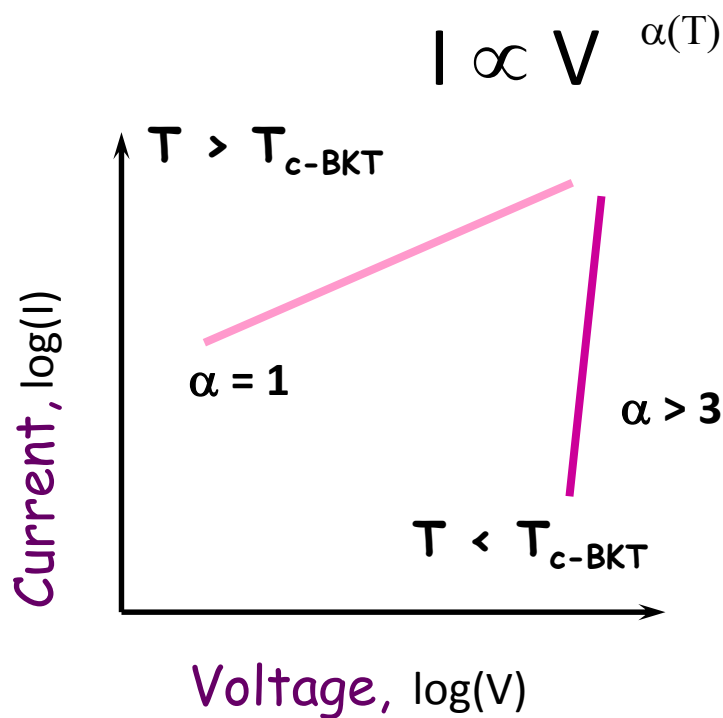
Rev. Mod. Phys., 59, 1001-1066 (1987).

$$\frac{2\pi n}{t} = \frac{1}{\lambda^2} - \frac{1}{\lambda_c^2}; \quad \lambda^{\sqrt{4t-1}} = \frac{1}{z} \left(1 - \frac{\lambda^2}{\lambda_c^2} \right); \quad t = \frac{T}{T_{CBKT}}; \quad n \propto \frac{G}{G|_{T=4T_{CBKT}}}$$



Current-Voltage Characteristics

in experiment:



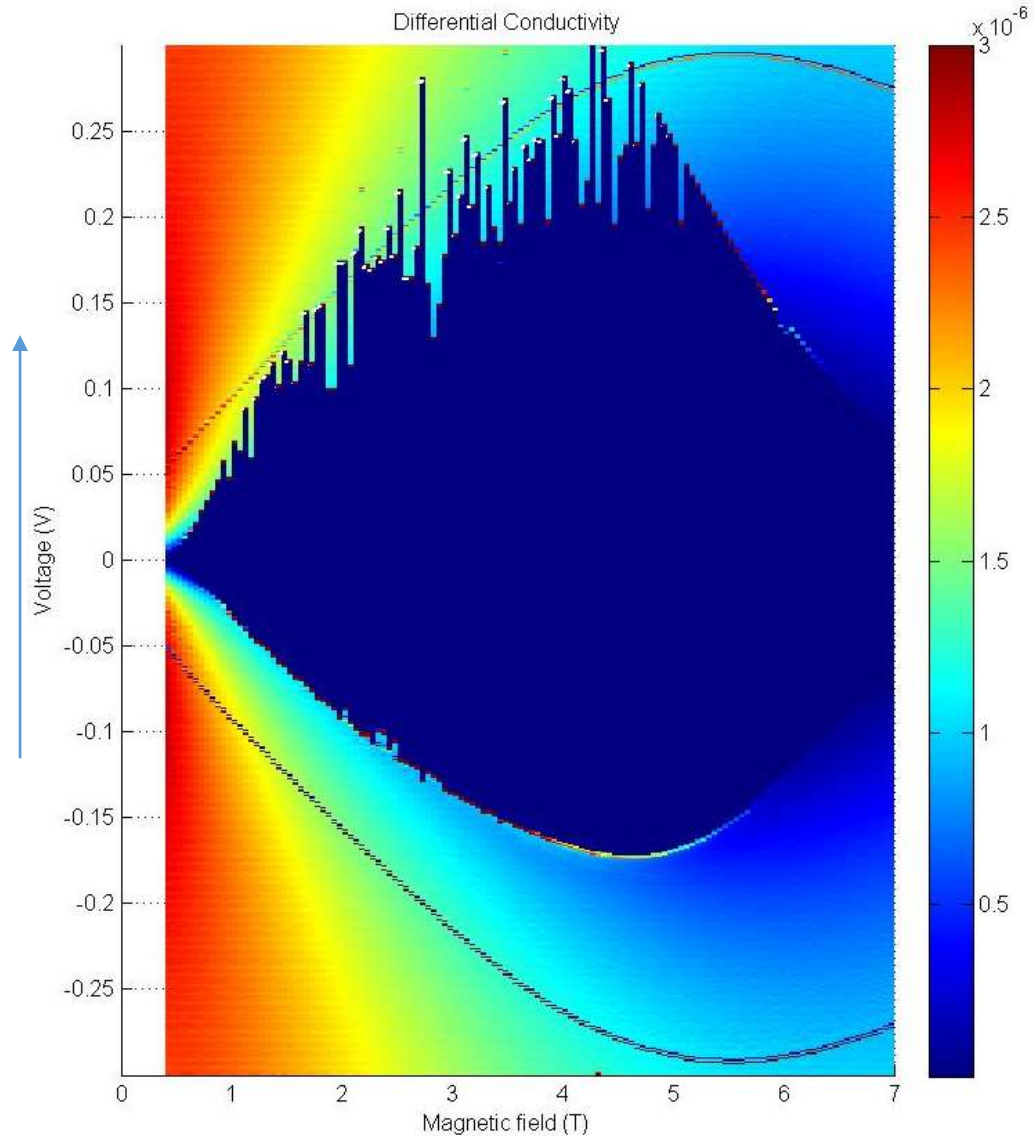
Sample NbTiN
 $d = 10 \text{ nm}$

Magnetic field evolution of differential conductivity

Temperature $T = 40 \text{ mK}$

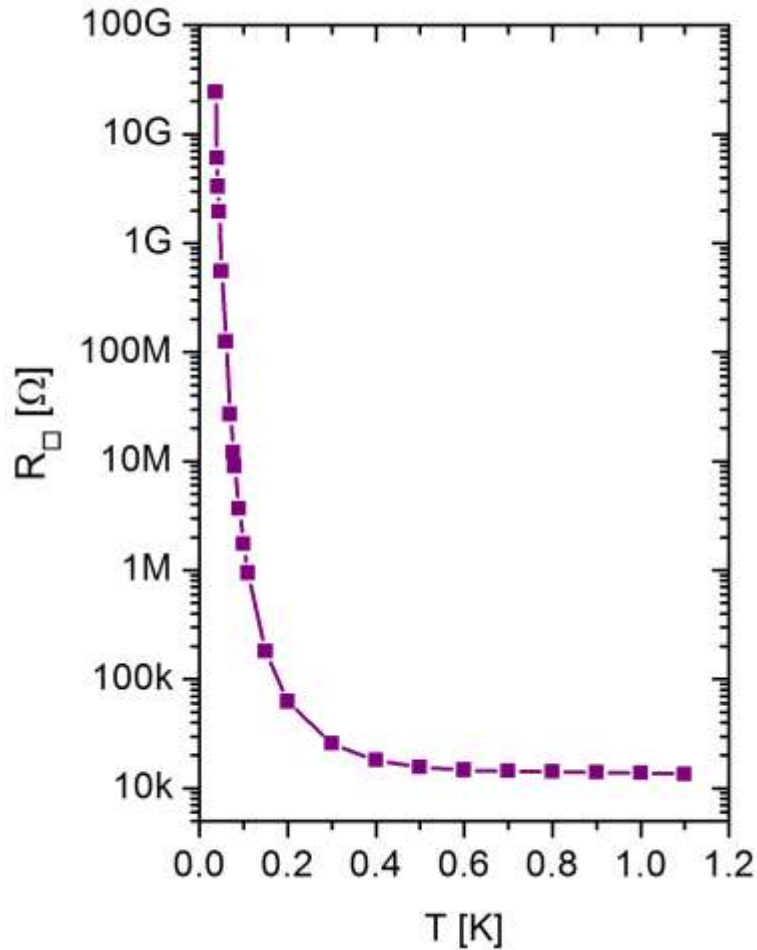
Collective insulating state:
Threshold behavior
of dI/dV vs V_{dc}

The threshold voltage
changes nonmonotonically
upon magnetic field

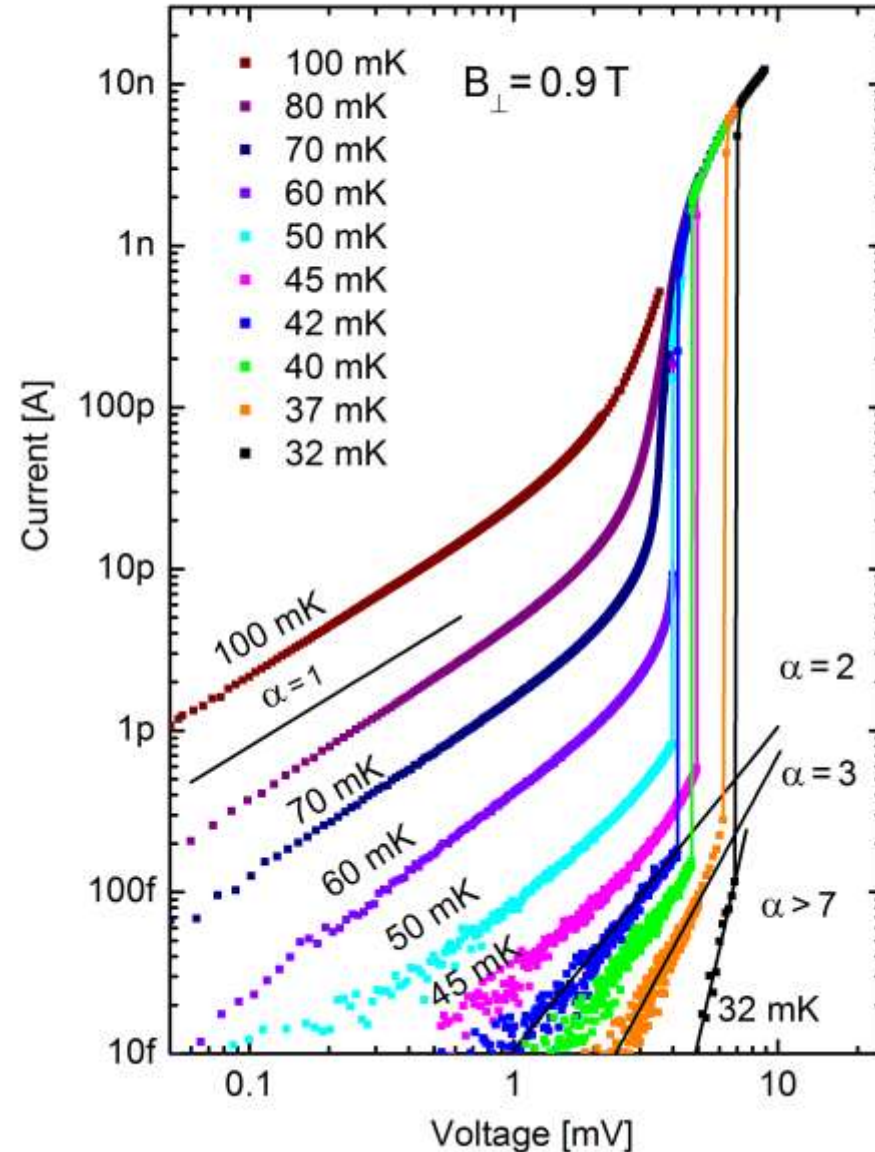


Charge BKT transition

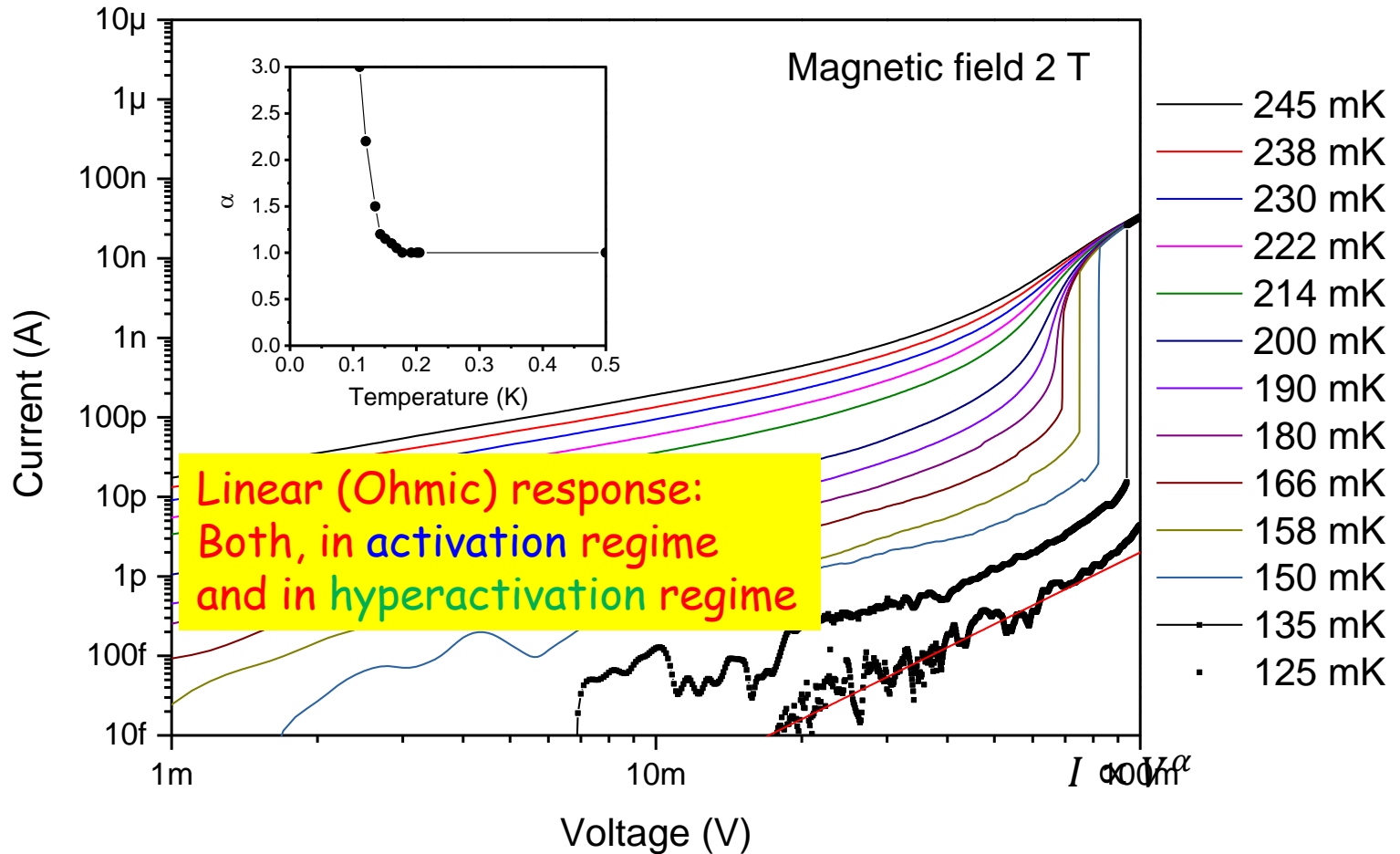
linear response regime



current - voltage characteristics



Charge BKT transition



heat balance equation

$$P = I^2 R(T_e) = \Sigma \Omega (T_e^\beta - T_{\text{ph}}^\beta)$$

Σ is the electron-phonon coupling constant

Ω is the volume of the sample

$R(T_e)$ is the sample resistance, which is assumed to depend only on the temperature of the electron subsystem, T_e

$\beta = n+2$, n is the power describing the temperature dependence of the electron-phonon relaxation rate:

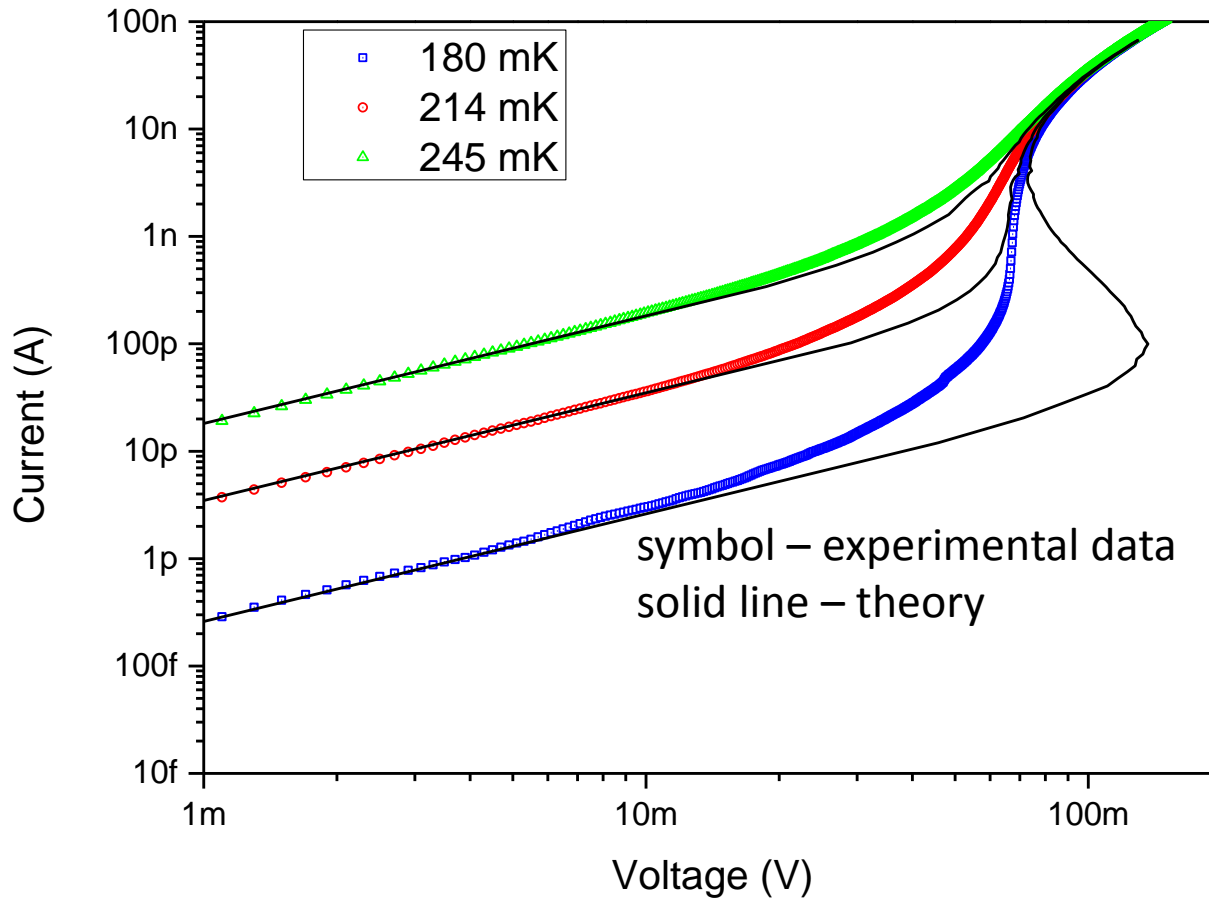
$$\tau_{e\text{-ph}}^{-1} \propto T^n$$

The value $n = 3$ ($\beta = 5$) was first calculated by V. F. Gantmakher [Rep. Prog. Phys. 37, 317 (1974)] and found in most metals.



Overheating?

the conventional overheating instability model well describes
nonlinear current-voltage characteristics
only in the **activation** regime

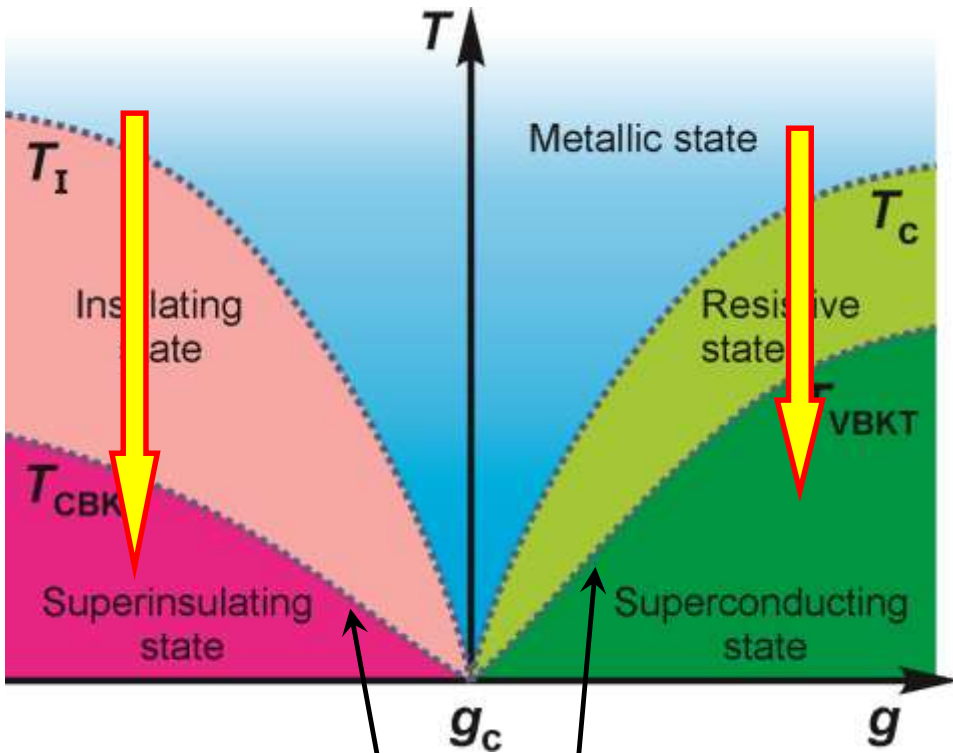


$$V^2 / R(T_{el}) = \Sigma \Omega (T_{el}^6 - T_{ph}^6)$$

Superconductor - Superinsulator Duality

Thermodynamic phase diagram

$$V \rightarrow 0, I \rightarrow 0$$



Topological phase transition

Dual current - voltage characteristics

